

DAWSON COLLEGE
Mathematics Department
Final Examination

Calculus II
201-NYB-05 (Commerce)

* WITH
ANSWERS *

Student Name _____

Student ID# _____

Instructors: Richard Bommier & Shahab Shahabi

TIME: 9:30 am - 12:30 pm

Answers to questions
above
are to be written directly
on the provided
paper in the provided
air dictionaries are
non-programmable
except where otherwise specified
in the examination paper.

ANSWER	
4/5	
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$$\int_{\mathbb{R}^n} \frac{1}{|x|^{\alpha}} dx = C_n \Gamma(\alpha + n) \cdot \frac{1}{\alpha + n}$$

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$$\int_{\mathbb{R}^n} \frac{x^2}{|x|^{\alpha+2}} dx = C_n \Gamma(\alpha + 3) \cdot \frac{1}{\alpha + 3}$$

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8. [5 marks]. Find the area of the region bounded by the graphs of the functions

$$f(x) := \sqrt[3]{x} \quad \text{and} \quad g(x) := x^2$$

Q. [5 marks]. Find the area of the region bounded by the graphs of the functions

$$y = x^2 + 1 \quad \text{and} \quad y = 3x^2$$

$$y = x^2 + x + 1$$

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$$\int_{-1}^0 (x^2 + x + 1) - (3x^2) dx$$

$$= \int_{-1}^0 (-2x^2 + x + 1) dx$$

$\infty \ln(n)$

THEOREM: CONVERGENCE TEST

$\frac{1}{n^p}$

$$\sum_{n=1}^{\infty} \frac{1}{n^p} < \infty \iff p > 1$$
$$\sum_{n=1}^{\infty} \frac{1}{n^p} = \infty \iff p \leq 1$$
$$\sum_{n=1}^{\infty} \frac{1}{n^p} \text{ DIVERGES}$$
$$\sum_{n=1}^{\infty} \frac{1}{n^p} \text{ CONVERGES}$$
$$\int_1^{\infty} \frac{1}{x^p} dx$$
$$\int_1^{\infty} \frac{1}{x^p} dx = \lim_{t \rightarrow \infty} \left[-\frac{1}{(p-1)x^{p-1}} \right]_1^t$$
$$= \lim_{t \rightarrow \infty} \left[-\frac{1}{(p-1)t^{p-1}} + \frac{1}{(p-1)} \right]$$
$$= \begin{cases} \infty & \text{if } p \leq 1 \\ \frac{1}{(p-1)} & \text{if } p > 1 \end{cases}$$

17. [5 marks]. Give an example (with a short justification) of a non-convergent

$$\sum_{n=1}^{\infty} \frac{1}{n^p} \text{ DIVERGES}$$