DAWSON COLLEGE Mathematics Department

FINAL EXAMINATION Calculus I- 201-NYA-05 (Open/Commerce) Fall 2021

Instructor: Noushin Sabetghadam

Student Name:	
Student ID. #:	

Instructions:

Print your name and ID in the provided space.

Solve the problems in the space provided for each question and show all your work clearly and indicate your nal answer(s).

Only calculators Sharp EL 531.X/ XG/XT are permitted.

This examination booklet must be returned intact.

This examination consists of 11 questions. Please ensure that you have a complete examination booklet before starting.

(1) Evaluate the following limits if possible and **write all the details**. (No marks is given if you use L'hopital Rules)

(a) (5 marks)
$$\lim_{x \neq 1} \frac{x - \frac{1}{x}}{x^2 - 8x + 7}$$

(b) (4 marks)
$$\lim_{x \neq 0} \frac{\sin(2x) \tan(3x)}{4x^2}$$

(c) (6 marks)
$$\lim_{x/1} \frac{P(x^2 + 7)}{x^2 + 3x} = 4$$

(2) (5 marks) Use only the limit de nition of the derivative to evaluate $f^{0}(x)$ where $f(x) = 3x^2 \quad 2x \quad 5$

(3) (4 marks) (a) Evaluate For which value(s) of a the function f

(4) (20 marks) Find the derivative. (Do NOT simplify)

(a)
$$y = \frac{2x^3 + 5x}{}$$

(d)
$$g(x) = 3^{(2x+1)} \arctan(x^2)$$

- (5) If $sin(y) + 3x^2y^3 = 5x$ y, then:
 - (a) (5 marks) $nd \frac{dy}{dx}$

(b) (2 marks) Find the tangent line to the graph of the given function at the point (0;0).

(8) **(6 marks)** A rectangular closed storage container is to have a base whose length is two times its width and a volume of 1440cm³. If the material for the base and top costs \$0:25 per cm² and the material for the sides costs \$0:10 per cm², nd the cost for the cheapest such container.

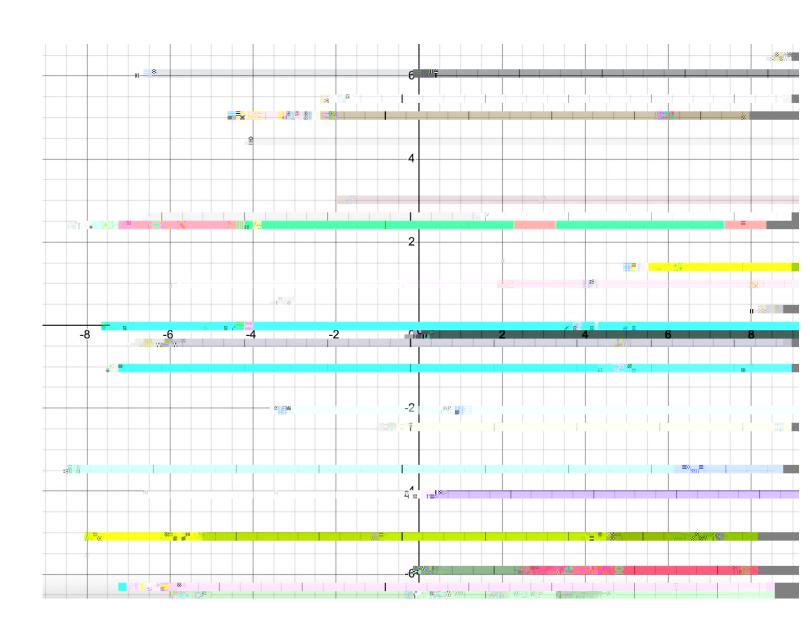
(9) **(5 marks)** Find the point(s) on the graph of the function $y = \frac{x^3}{(x^2 - 1)^2}$ where the tangent line is horizontal.

(10) (5 marks) Let $f(x) = \frac{\ln x}{x}$, Find $f^{(0)}(x)$ and then evaluate $f^{(0)}(e)$.

(11) Given the function $f(x) = \frac{x^2 - 2}{4}$

(d)	(3 marks) Find the intervals where the function f nd its relative maximum point(s) and relative	is increasing or decreasing and also minimum point(s) if there is any.
(e)	(3 marks) Find the intervals where the function and also nd its in ection point(s) if there is any	

(f) (2 marks) Use all the data collected about f to draw the its graph in the coordinate system below.



Final Answers

(1) (a)
$$\frac{1}{3}$$

(b)
$$\frac{3}{2}$$

(c)
$$\frac{1}{4}$$

(2)
$$f^{\theta}(x) = 6x$$
 2

(3) (a)
$$a = 2$$

(b)
$$\frac{7}{3}$$

(4) **(a)**
$$y^0 = 3$$

$$\frac{2x^3 + 5x}{3x^5 + 2x} = \frac{2(6x^2 + 5)(\sqrt{3x^5 + 2x})}{(3x^5 + 2x)} = \frac{15x^4 + 2}{2\sqrt{3x^5 + 2x}}(2x^3 + 5x)}{(3x^5 + 2x)}$$

(b)
$$f^{\emptyset}(x) = 2\cos(x^2 + 3)2x\sin(x^2 + 3) + 3\sec^2(\log_2 x)\frac{1}{x\ln 2}$$

(c)
$$y^{0} = (1 + \ln x)^{\sec x} [\sec x \tan x \ln(1 + \ln x) + \sec x \frac{\frac{1}{x}}{1 + \ln x}]$$

(d)
$$g^{\emptyset}(x) = 2 \ln 3 \ 3^{(2x+1)} \ \arctan(x^2) + \frac{2x}{1+x^2} \ 3^{(2x+1)}$$

(5) (a)
$$y^0 = \frac{5 + 6xy^3}{\cos y + 9x^2y^2 + 1}$$

(b)
$$y = \frac{5}{2}x$$

(6) (a)
$$P(x) = 0.004x^3 + 0.9x^2 + 1200x$$
 16000

(7)
$$\frac{dx}{dt}$$
 48.97 mph

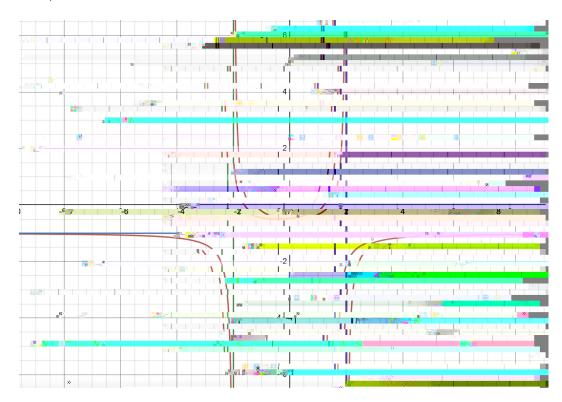
(10)
$$f^{\emptyset}(x) = \frac{2 \ln x}{x^3}$$
; $f^{\emptyset}(e) = \frac{1}{e^3}$

(11) (a) D(f) = R n f 2;2g

(b)
$$(\stackrel{\mathcal{O}}{\overline{2}}; 0); (\stackrel{\mathcal{O}}{\overline{2}}; 0); (0; 1=2)$$

(c)
$$x = 2$$
; $x = 2$; $y = 1$

- (d) f is increasing on (0;2) [(2;1) and decreasing on (1;2) [(2;0)]. There is a relative min at (0;1=2).
- (e) f is concave upward on (2;2) and downward on (1;2) [(2;1). There is no in ection point.



(f)